

E157 Lecture 6 Day Plan

Any questions before quiz

Quiz + Team Quiz + Talk through solution

Q roundup

- Bandpass fractional bandwidth = $1/Q$
- RLC ring down in step/impulse response \sim number of peaks to 5% = Q
- Series RLC $Q = \sqrt{L/C} / R$
- Parallel RLC $Q = R / \sqrt{L/C}$
- Series component $Q = X/R \leftarrow$ This is frequency dependent! Not a full tank!
- Parallel component $Q = B/G$
- Can find a compound Q by mixing components
 - \rightarrow Parallel LC where both cap and inductor have ESR
 - \rightarrow draw schematic and do series-parallel drawign

Calculating Compound Q from components

- Same circuit as above
- $X_S = X_P \cdot Q^2 / (Q^2 + 1)$, $R_S = R_P / (Q^2 + 1)$,
- Q here is from each element, but we know ω_0 will be $1/\sqrt{LC}$.
 - $Q_1 = 1/\omega_0 R_C = \sqrt{L/C} / R \leftarrow$ still IM/RE because series elements
 - $Q_2 = \omega_0 L / R = \sqrt{L/C} / R$
- Transform, then overall is $(R_S R_C P \parallel R_S R_L P) / \sqrt{L/C}$
- NOTE that X_s is always $< X_p$ and R_s is always $< R_p$

Practice ringing out in shunt – 50 ohm || 10pF || 100nH @1Grad/s – see below

- You are designing a matching network for a 10pF capacitor in shunt with a 50 Ohm resistor driven by a 1Grad/s signal sent through a 50 Ohm transmission line.
- $B_n = \omega C / (1/Z_0) = Z_0 \cdot \omega \cdot C = 0.5$
- Need negative susceptance, so shunt L
- $B_n = 1/\omega L / (1/50) = 50/\omega L \rightarrow 100\text{nH}$
- $Q = R / \sqrt{L/C} = 50/\sqrt{100\text{e-}9/10\text{e-}12} = 50/\sqrt{1\text{e}4} = 5$
- $\sqrt{1/LC} = 1\text{Grad/s} \rightarrow L \cdot 1\text{e-}11 = 1\text{e-}18 \rightarrow L=100\text{nH}$

Some practical stuff

- Emphasize that networks of bypass caps exist to manage ESR and ESL.
- Also mention winding resistance for inductors