

E151 Lecture 1 – Intro and Linear Networks Review

Matthew Spencer
Harvey Mudd College
ENGR151

Disclaimer

These are note for Prof. Spencer to give the lecture, they were not intended as a reference for students. Students asked for them anyway, so I'm putting them up as a courtesy. Remember that they are not intended as a substitute for lecture.

Why Take This Class

- Teaching analog circuit design
- “Analog is dead and digital is king” – some strawman
- Used ADC in E80, why not apply to every analog problem? (board list)
 - Speed, noise, dynamic range, power ← All tightly linked
 - Expensive, complex to design and use, delicate
 - Why is outside the scope of this class ... but true
- What other analog tool do you know (op-amp). Why not? (board list)
 - Low power output
 - Limited bandwidth
 - We WILL learn why here ← YOU WILL BUILD ONE

Goals and How We'll Get There

- Learning goals: you will learn how to build an op-amp (as list)
 - Really good at basics: RC dynamics and KVL/KCL
 - Basic semiconductor physics and intuition for how devices work in circuits
 - Single and multi-stage linear amplifiers
 - Analog building blocks and “talking the talk”
 - Fearless in lab and rational debugging
- Organized as: Large signal / Small signal / Dynamics / Other Stuff
- Learning and note taking
 - Transparent teaching
 - Frequent low stakes assessment and interleaved practice
 - Lecture feels good, but activities are how you make knowledge stick
 - Notes during derivations

How Are We Doing This?

Mon	11:59PM	Turn in Lab Notebook & Problems
Tue	Lecture	Lab debrief
Tue	11:59PM	Turn in warm-up problems
Wed		
Thu	12:01PM Lecture	Turn in self-graded problems Quiz on lecture material (ind, + group)
Fri	Lab	Oscope lesson & work time

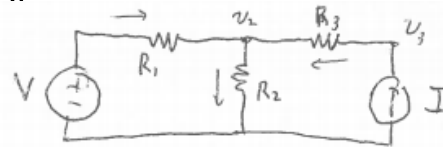
- Lab deliverable is notebook: next slide
- Problems don't need to be done before lab, just related
- More later on design project, problems solo, DP + lab partners

Lab Notebook Demo

- My example posted on the website.
- Necessary features
 - Chronological – that helps you reference when your boss asks a q
 - Informal and handwritten parts – clear, but not a writeup, always evidence
 - Contains necessary data – doesn't have to be at end like this, but highlight
 - Contains convincing evidence of experiments – need to be able to replicate from it
- Notebooks are important: This should help you both in and out of lab
- You need to get right measurements in this class, like 80
- Lab password
- Break to gather partners, come back to tech work.

E84 was Linear Circuit Theory

- Small groups, find i_2 3 different ways for



① KCL $i_2 = \frac{V - v_2}{R_1} + I$ & $v_2 = i_2 R_2 \rightarrow i_2 = \frac{V}{R_1} - \frac{i_2 R_2}{R_1} + I$

$$I = \frac{v_3 - v_2}{R_3}$$

$$i_2 \left(1 + \frac{R_2}{R_1}\right) = \frac{V}{R_1} + I$$

$$i_2 = \frac{\frac{V}{R_1} + I}{1 + R_2/R_1}$$

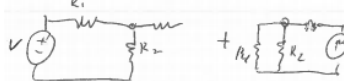
② KVL

$$V = i_1 R_1 + (i_1 + I) R_2$$

$$i_1 = \frac{V - I R_2}{R_1 + R_2}$$

$$i_2 = \frac{V + I R_1}{R_1 + R_2} = \frac{V/R_1 + I}{1 + R_2/R_1}$$

③ Superposition



$$i_2 = \frac{V}{R_1 + R_2} + I \frac{R_1}{R_1 + R_2}$$

Split into "superposition subcircuits" and "turn off" supplies

- Splitting into equivalent summed circuits really common in 151
- Why the heck do we "turn off" sources

Matrix Picture of Circuit Linearity

- Split matrix into vectors and turn them off one at a time.

$$\begin{bmatrix} V \\ v_2 \\ v_3 \end{bmatrix} = \begin{bmatrix} R_1 & R_2 & 0 \\ 0 & R_2 & 0 \\ 0 & R_2 & R_3 \end{bmatrix} \begin{bmatrix} i_1 \\ i_2 \\ I \end{bmatrix} = \begin{bmatrix} R_1 \\ 0 \\ 0 \end{bmatrix} i_1 + \begin{bmatrix} R_2 \\ R_2 \\ R_2 \end{bmatrix} i_2 + \begin{bmatrix} 0 \\ 0 \\ R_3 \end{bmatrix} I$$

Can find I contrib. Takept R_1 & R_2

① Make superpos subccts by "turning off" all but I src (short/open)

② Find i_2

③ Sum across all superpos subcct

Dependent Sources (I solve)

- V source or I source controlled by some other spot in circuit

Dependent Sources

$\diamond kV$ $\diamond g_m V$

- generate a voltage or current depending on some other V or i in ckt

→ we this, just have resistors, transformers

• Can't use superposition b/c depends on another source
 ↳ must be in all superpos sub ckt.

@ eliminate w/

Solve

$$\frac{V - i_2 R_2}{R_1} + g_m R_2 i_2 = i_2$$

$$\frac{V}{R_1} = i_2 \left(1 + \frac{R_2}{R_1} - g_m R_2 \right)$$

$$i_2 = \frac{V/R_1}{1 + R_2/R_1 - g_m R_2}$$

- Can get crazy results (feedback)
 - Can get hairy algebra

Thevenin

- Don't care about circuits floating in space – want to connect them
- Connecting them to stuff can cause loading, need i-v relationships
- Place we make a connection called a port (where we apply vt) eg:

What is i-v relation across port?

- must be linear
- model may have DC value
- model w/ src + res

i_{sc} v_{oc} $\frac{1}{R_{TH}}$ b/c rise is current

Norton is V-I curve instead of I-V

Thevenin

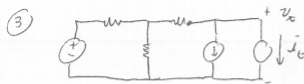
Norton

Example Find Thevenin Impedance 2 Ways

- Options: voc/isc (slope), simplify network (why does that work?)
- Then I show 3rd way: test sources (derivative of circuit)

① $v_{oc} = v_3 = I(R_3 + R_1 \parallel R_2) + V \frac{R_2}{R_1 + R_2}$ by super pos $R_{TSC} = I + \frac{V}{R_3 + R_1 \parallel R_2} \cdot \frac{R_2}{R_1 + R_2}$

② $R_{TH} = R_3 + R_1 \parallel R_2$ w/ shorted & opened sources



- can pick current or voltage test
- ask how much i or v out (find di/dv)
- I easy here b/c \parallel w/ I

$$v_o = V \frac{R_2}{R_1 + R_2} + (I + i_t)(R_3 + R_1 \parallel R_2)$$

- **MUST** use this technique w/ dep. src.

$$\frac{dv_o}{di_t} = R_3 + R_1 \parallel R_2 \text{ (eq to small signal model, setting } v_o \text{ to } 0)$$

[super handy for figuring tricky circuit details!]

MUST SHUT OFF SOURCES for di/dv . (Small wiggles go to die)