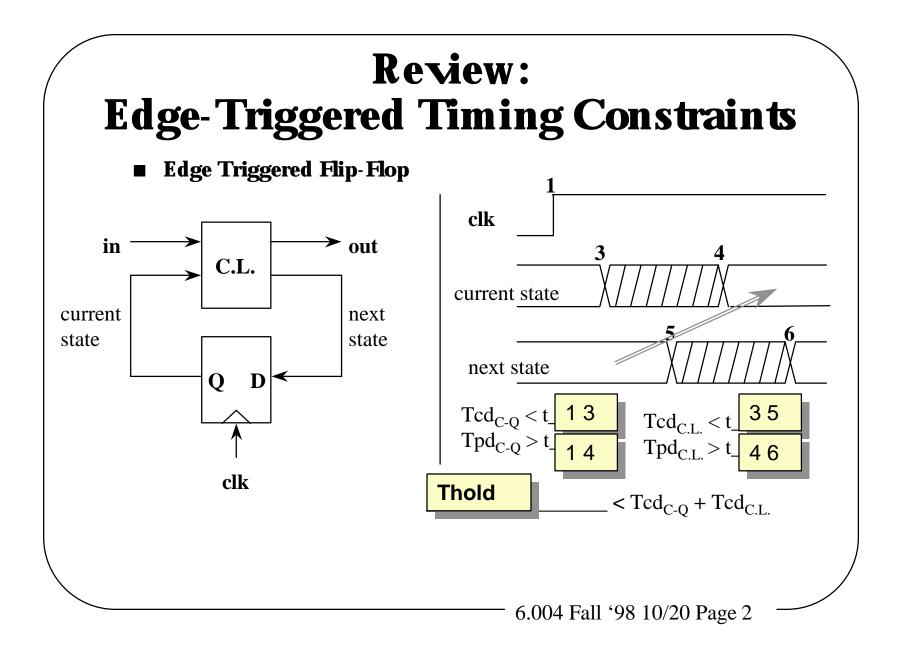
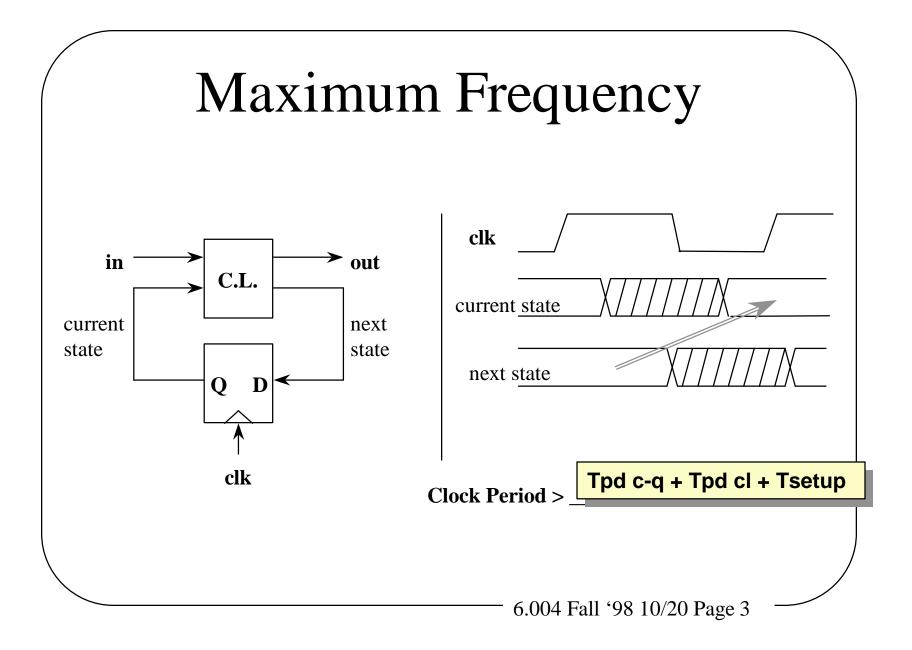
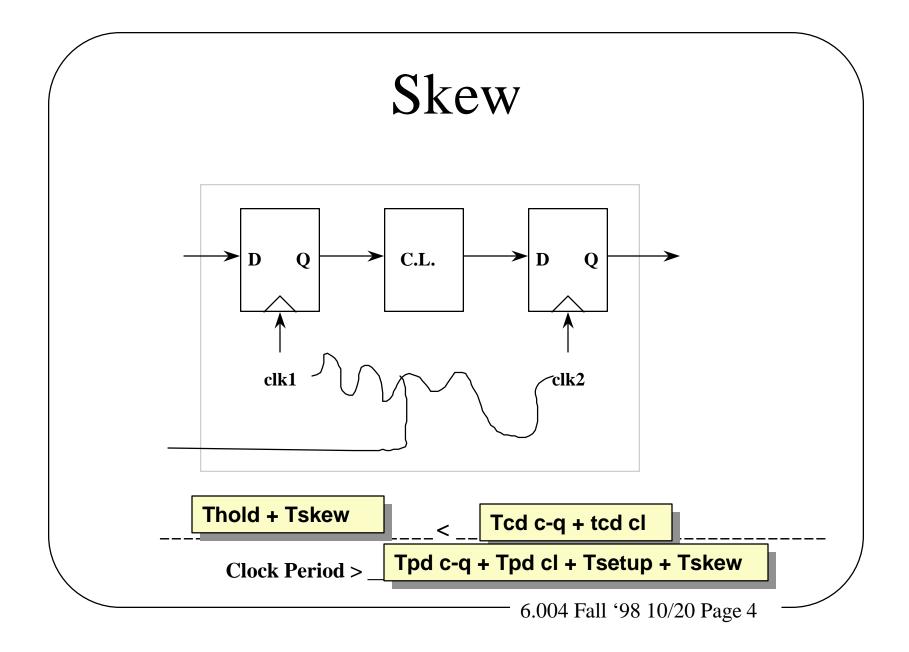
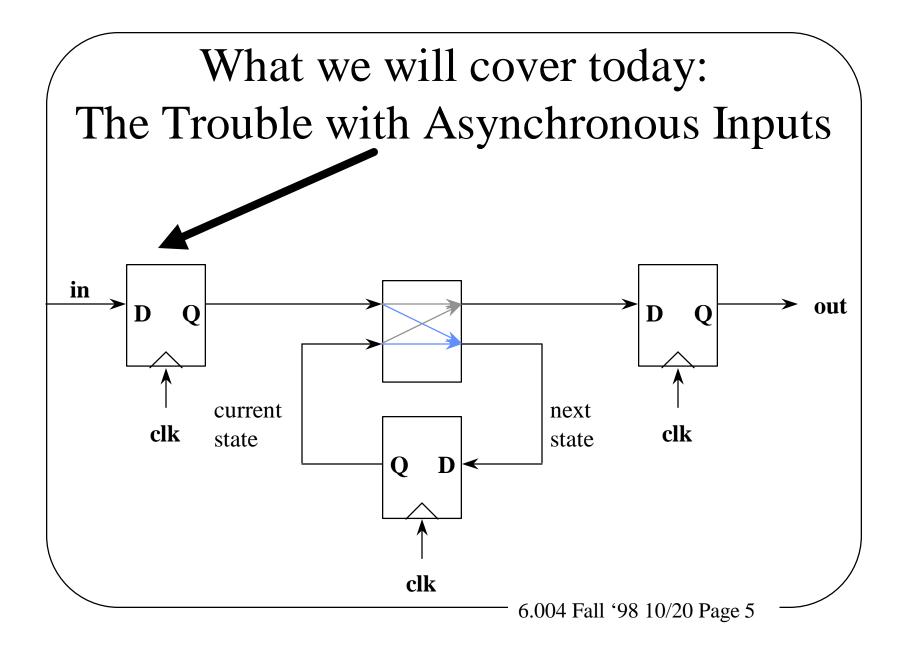
**6.004 Fall '98** L11: Arbitration, Synchronization, and Metastability

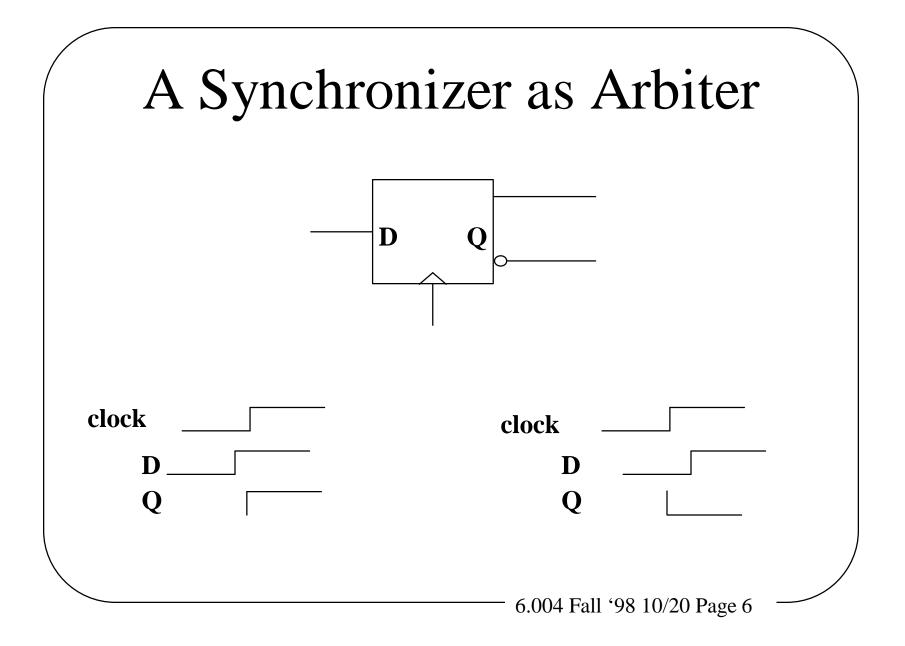
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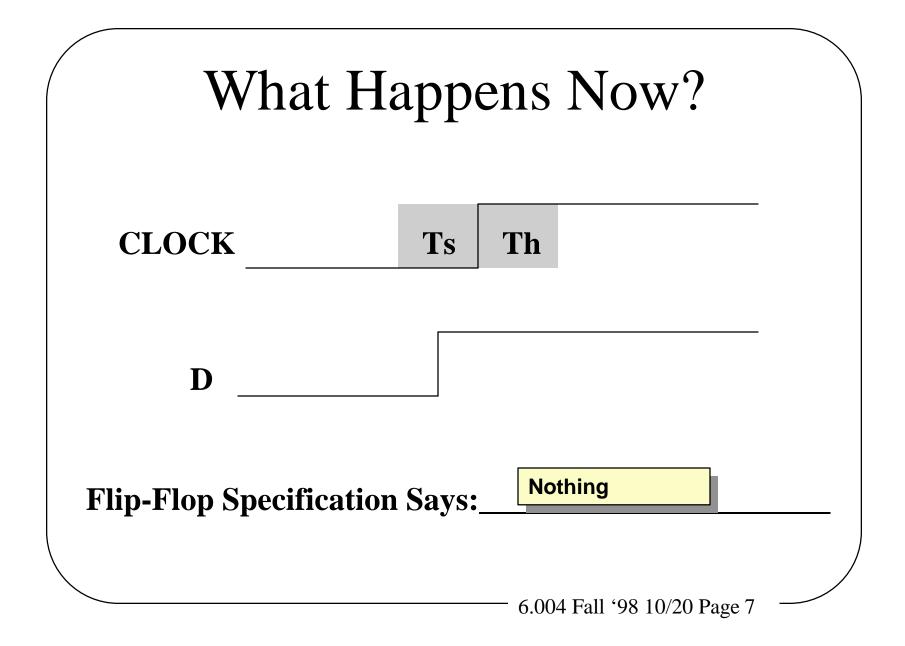




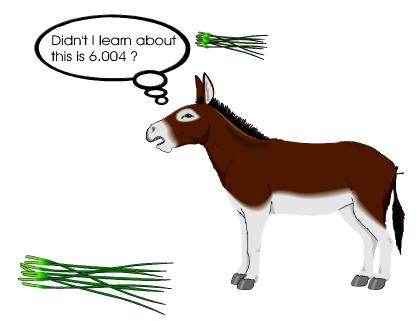








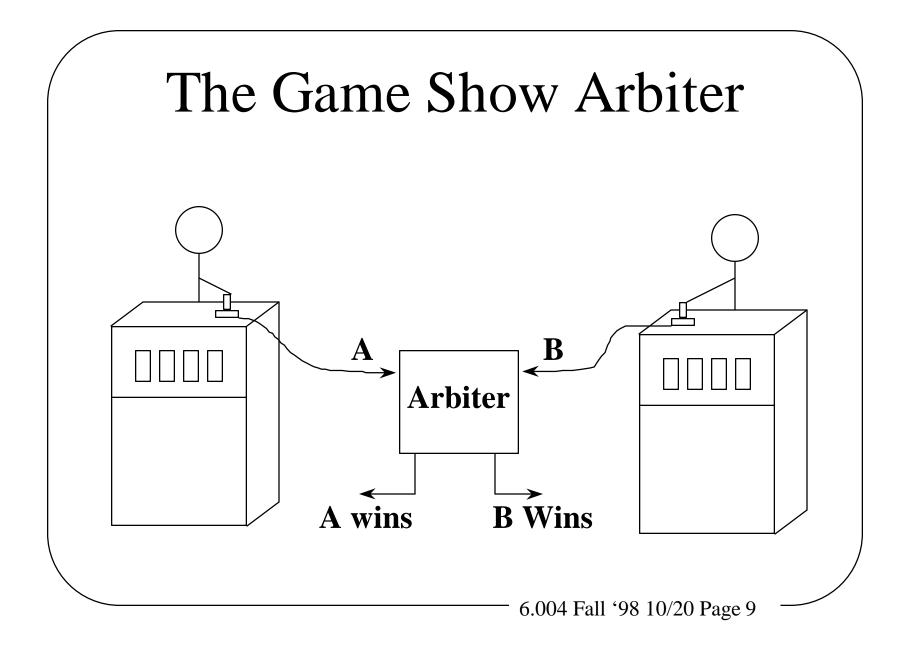


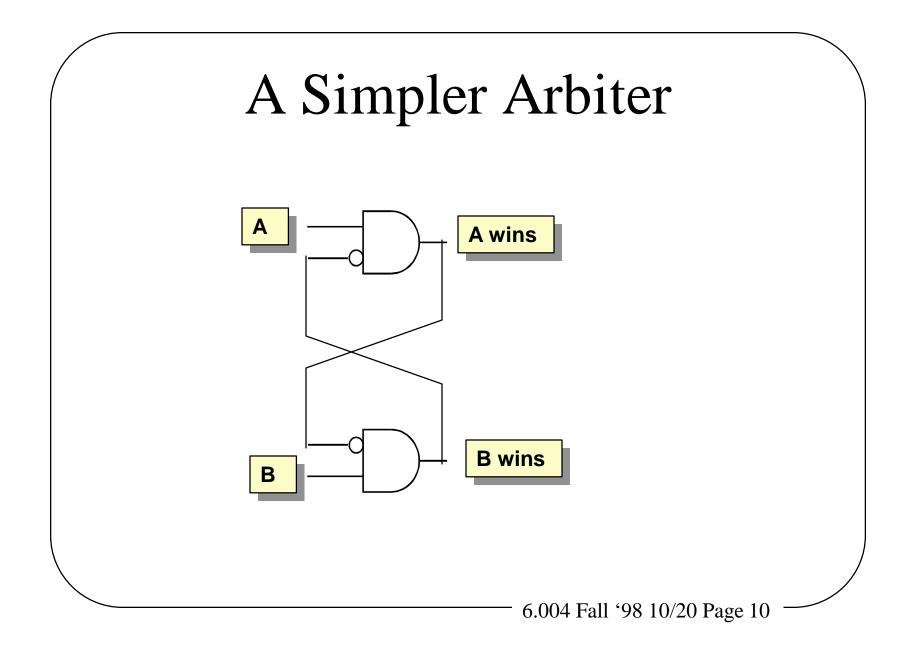


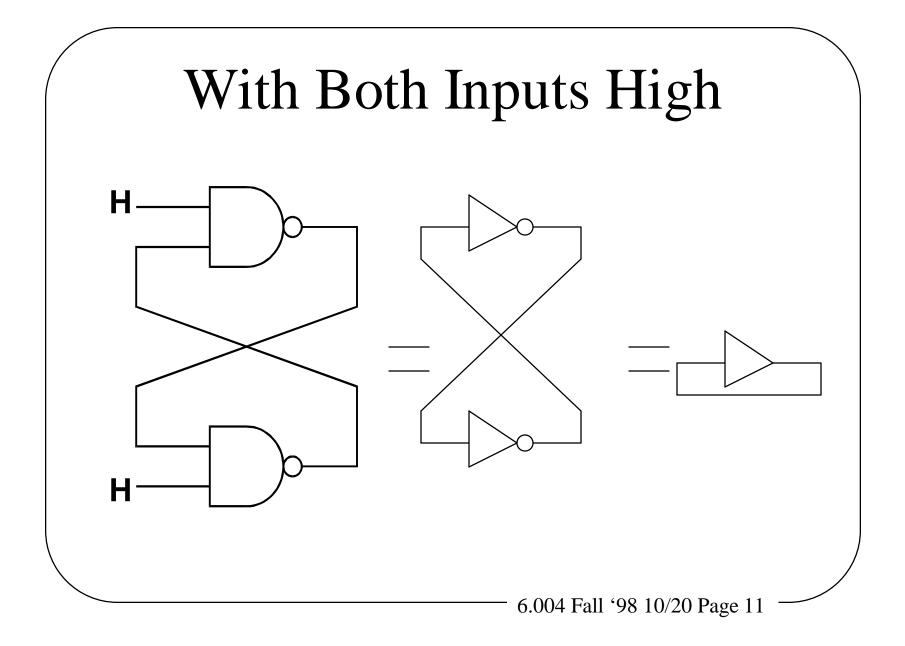
Buridan, Jean

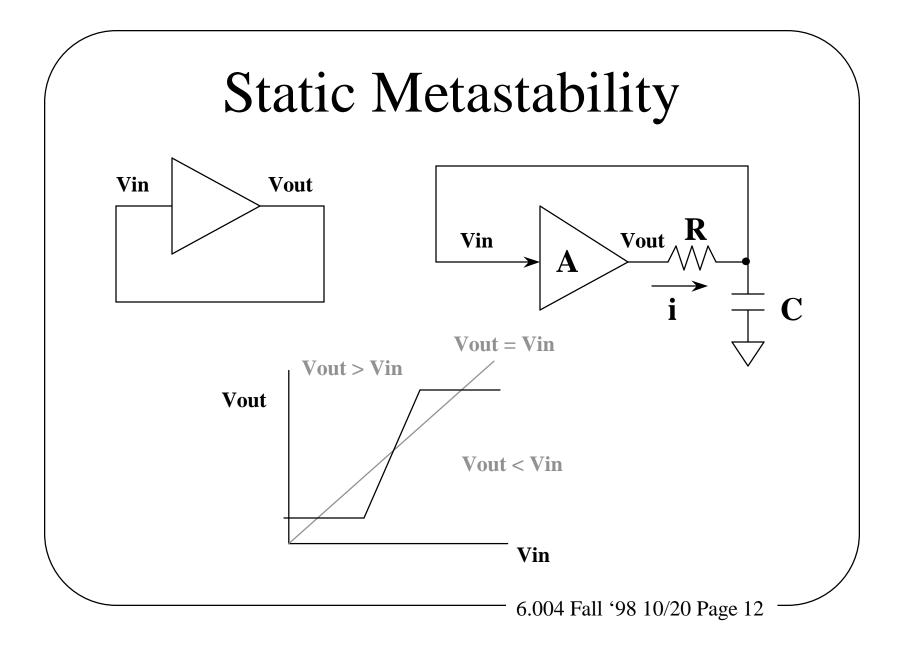
Buridan, Jean (1300-58), French Scholastic philosopher, who held a theory of determinism, contending that the will must choose the greater good. Born in Bethune, he was educated at the University of Paris, where he studied with the English Scholastic philosopher William of Ockham. After his studies were completed, he was appointed professor of philosophy, and later rector, at the same university. Buridan is traditionally but probably incorrectly associated with a philosophical dilemma of moral choice called "Buridan's ass." In the problem an ass starves to death between two alluring bundles of hay because it does not have the will to decide which one to eat.

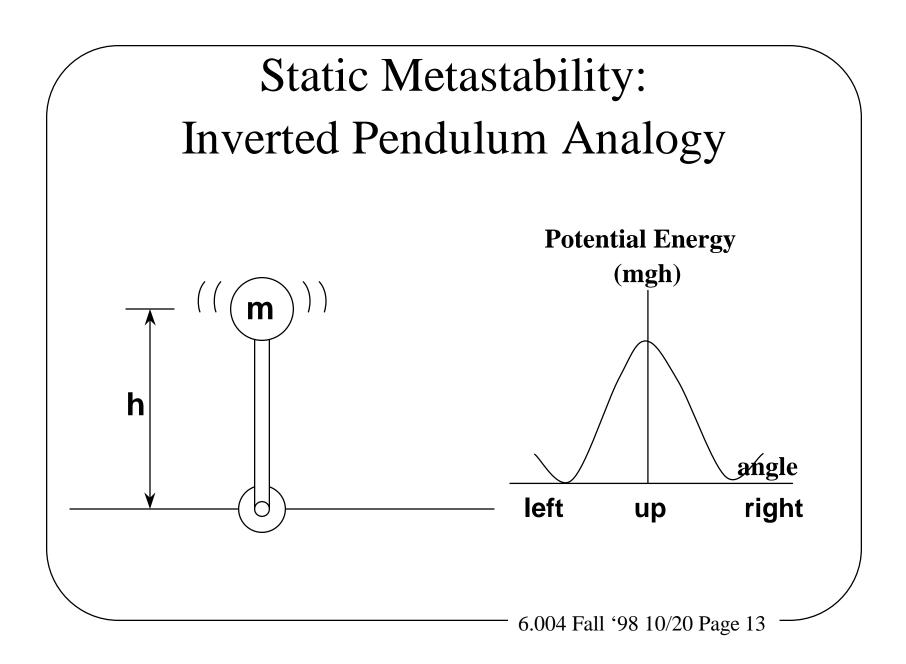
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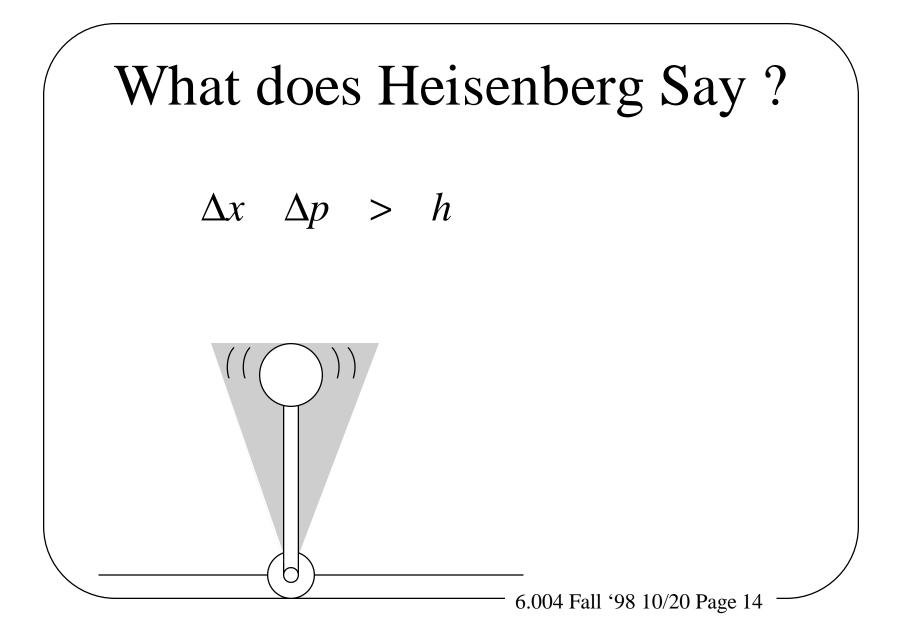


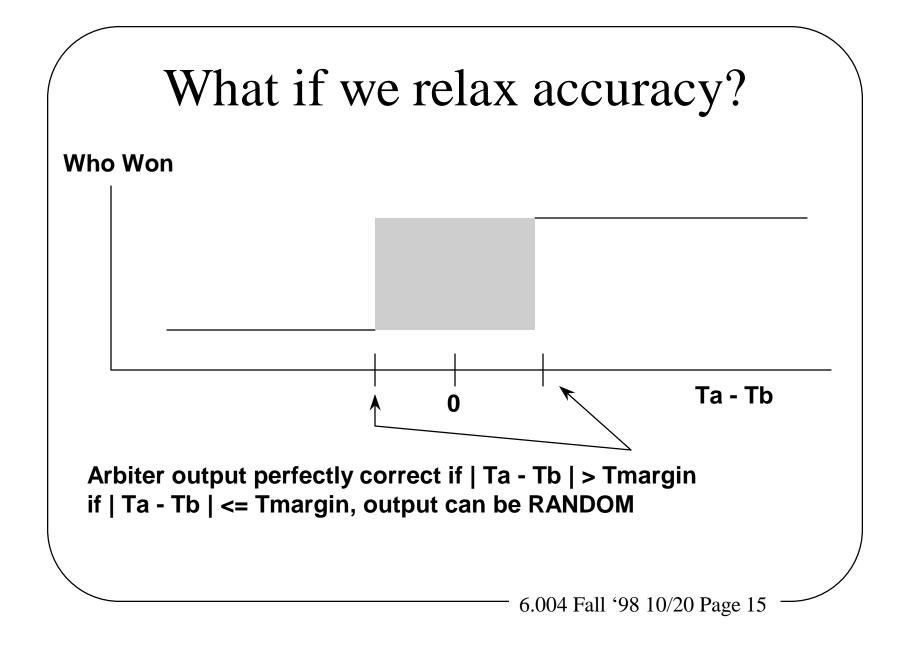


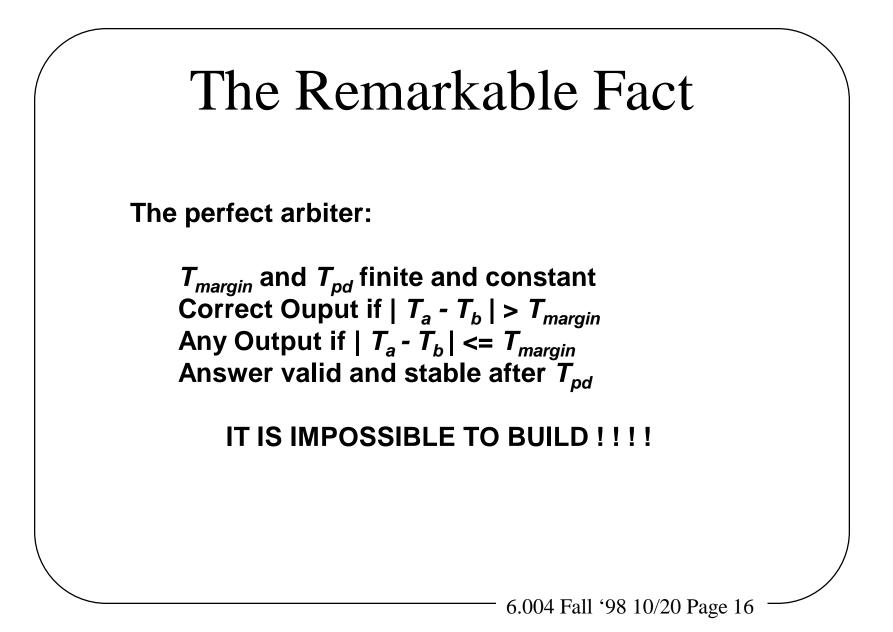


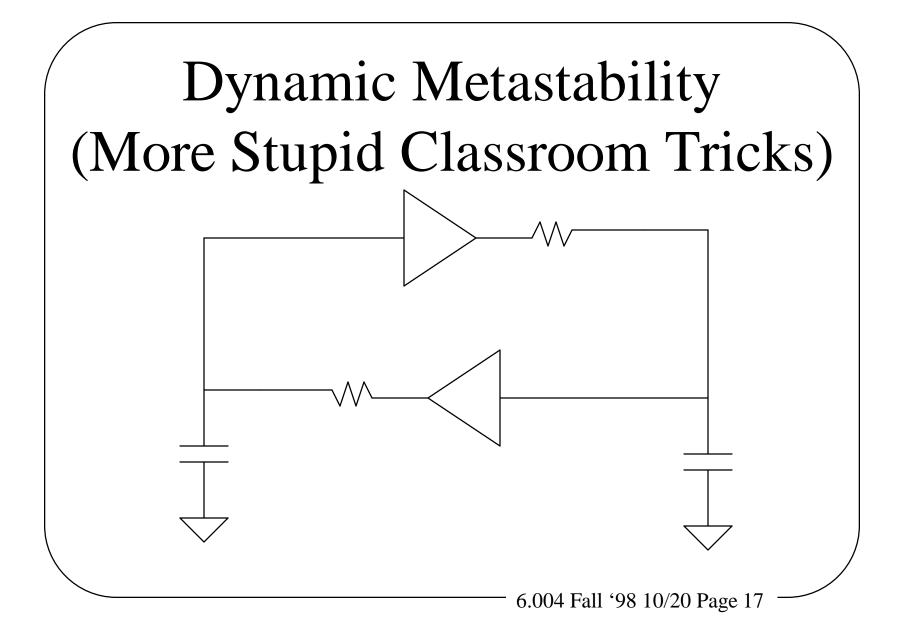


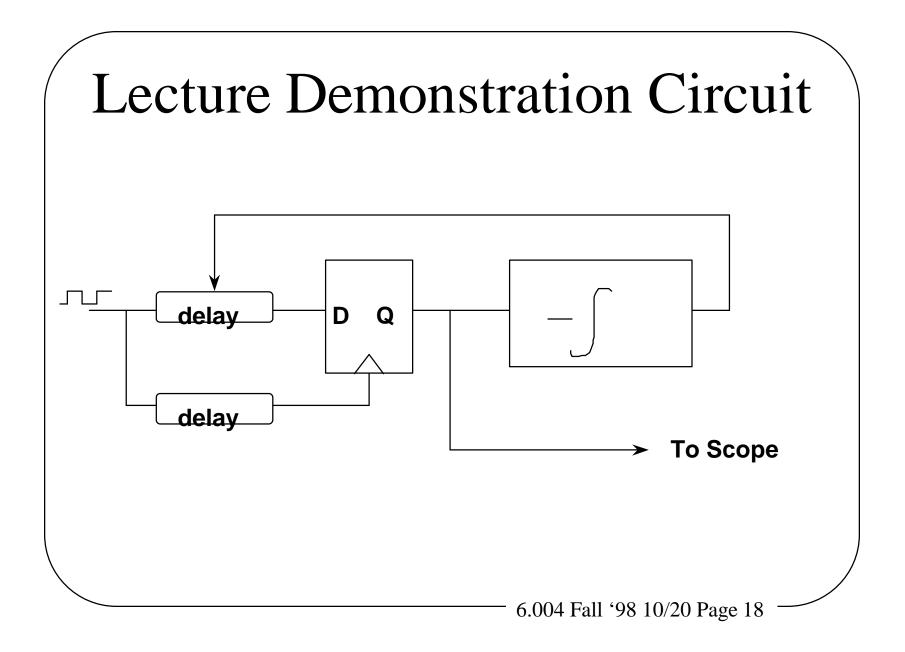


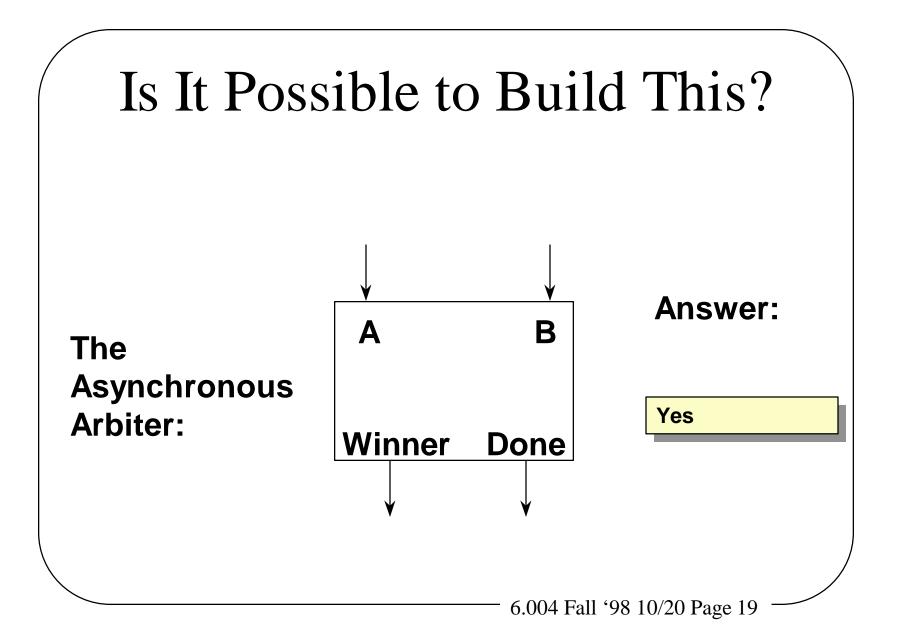


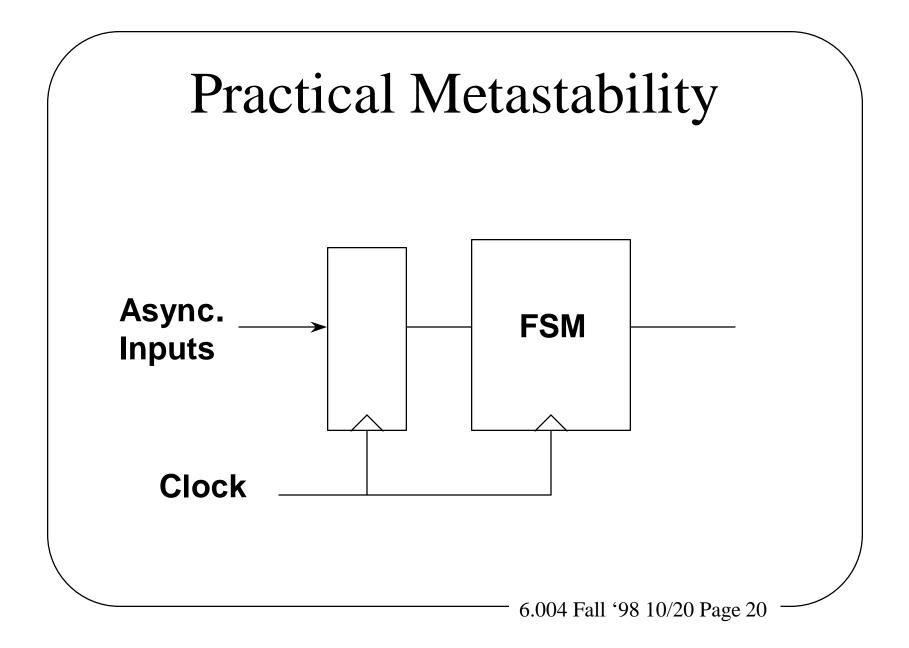


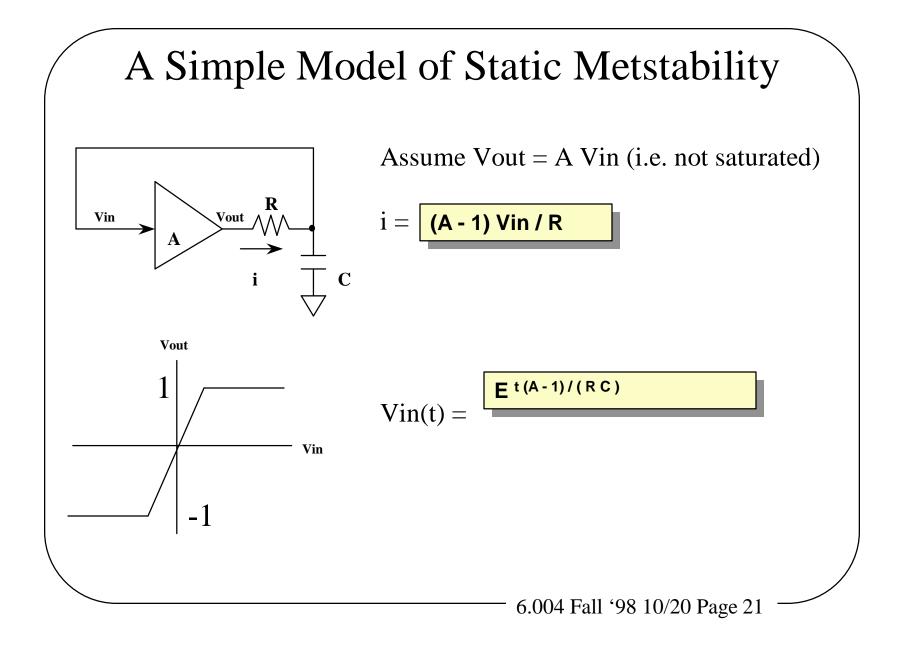


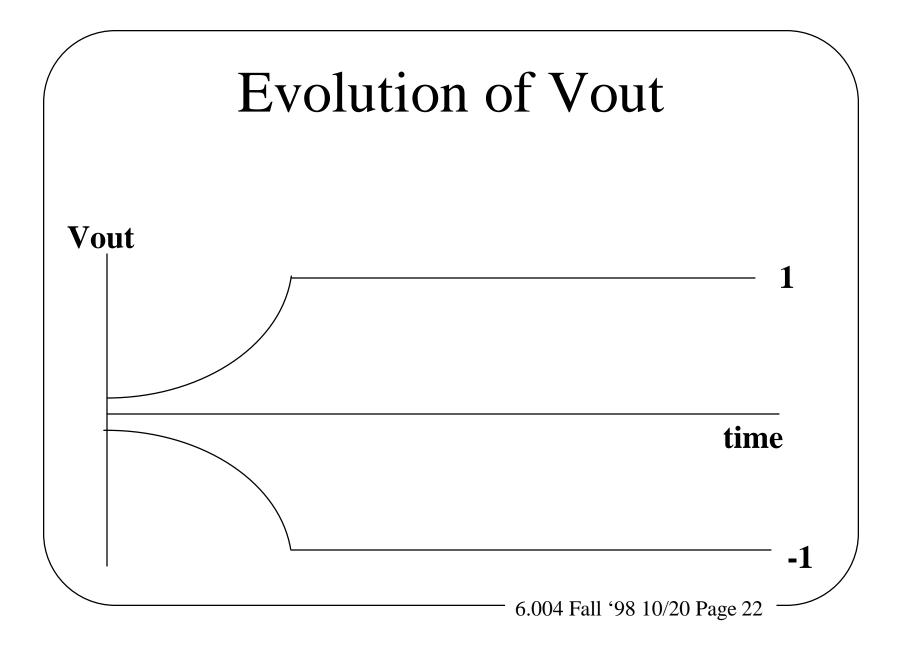


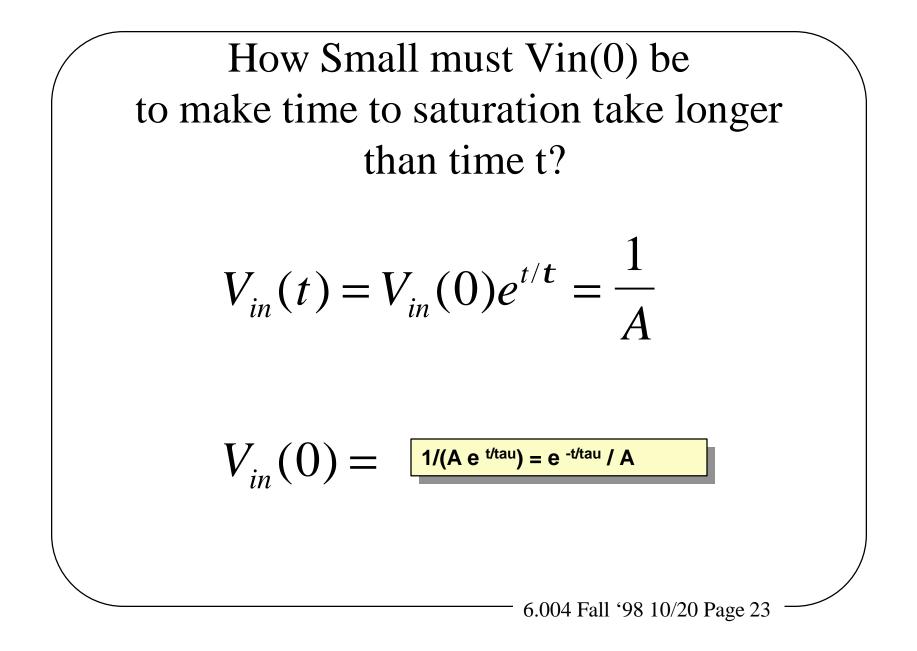


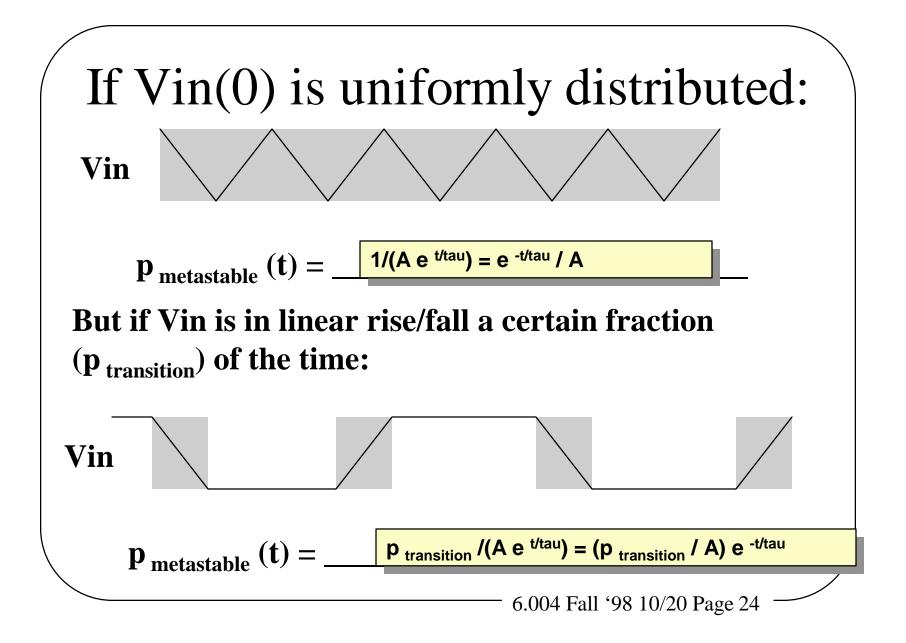


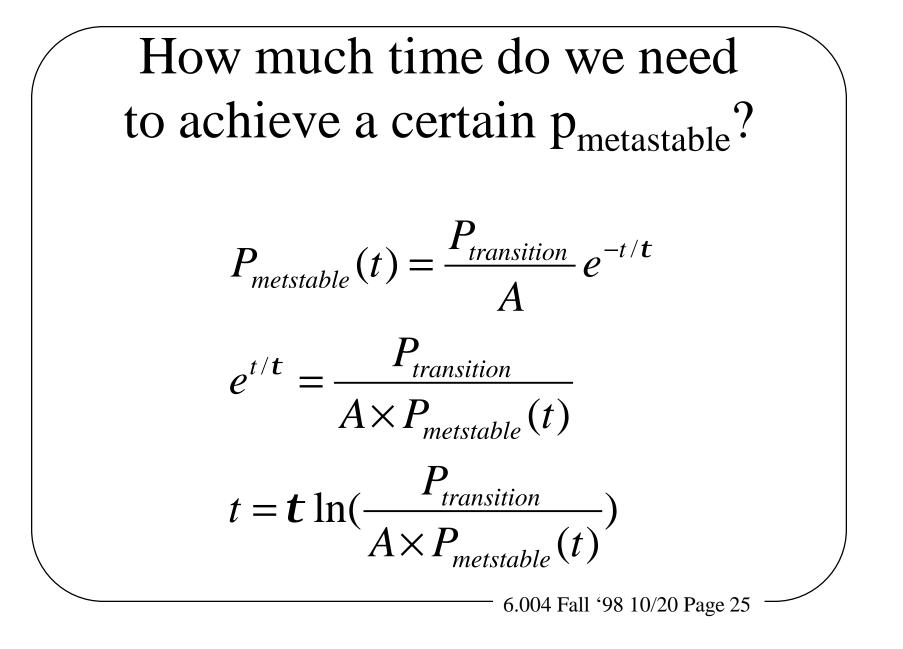






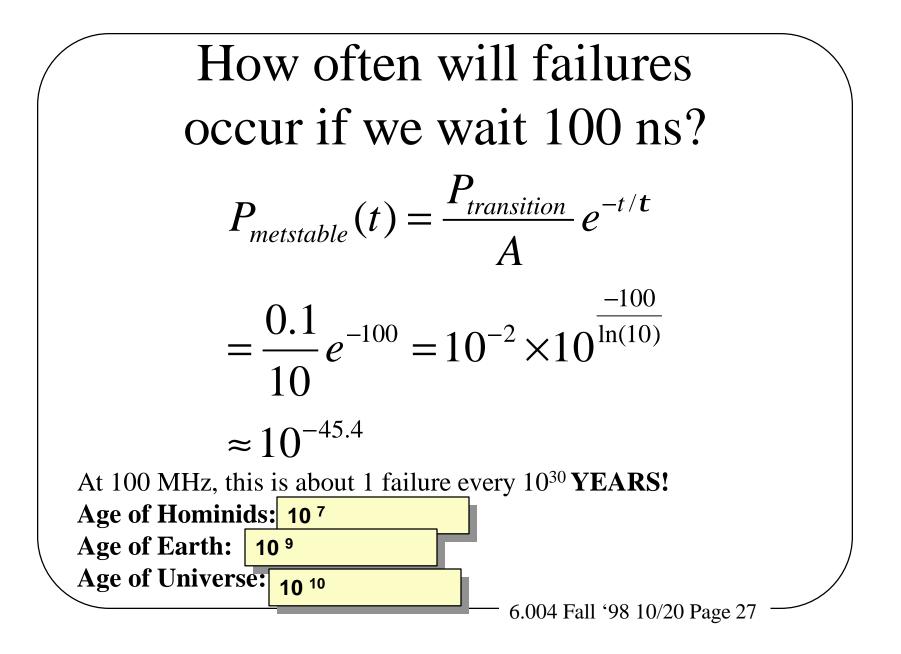


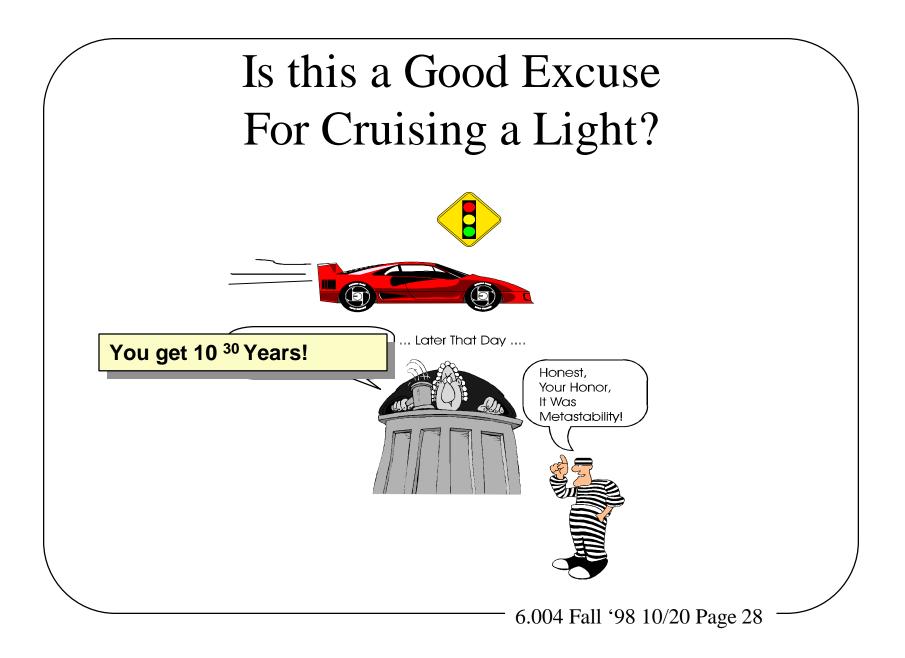




Example:  
How Long for 1 failure / year?  
100 MHz Clock (t = 10 ns)  

$$p_{\text{transition}} = 0.1$$
  
 $A = 10$   
 $\tau = 1 \text{ ns}$   
 $P_{\text{metstable}} = \frac{P_{\text{transition}}}{A} e^{-t/t}$   
 $t = t \ln(\frac{P_{\text{transition}}}{A \times P_{\text{metstable}}})$   
 $P_{\text{metstable}} = 1 / (100 \text{ MHz} \cdot 1 \text{ year})$   
 $= 1 / (10^8 \text{ x } \pi \text{ x } 10^{-7}) = \pi \text{ x } 10^{-16}$   
 $t = 10^{-9} \ln(0.1 / (10 \text{ x } \pi \text{ x } 10^{-16})) = \text{about } 31 \text{ ns}$   
How about 10 years instead of 1?  
 $t = (10^{-9})\ln(\text{pi x } 10^{\circ}(-15)) = 33ns$   
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## What did we Learn Today?

- If we violate setup or hold times, a flip-flop can give a random digital output.
- If we violate setup or hold times, we can't bound the propagation delay of a flip-flop.
- Metastability usually causes strange outputs, but flip-flops are sold that have valid, stable, outputs while internal nodes are metastable. They can still change their minds when coming out of metastability.
- In practice, we can choose a propagation time that will have a forever stable output "most" of the time.
- If we wait long enough (typ. 10-100 ns) "most of the time" is almost all of the time.
- We can easily detect when settling happens, but we can't say how long it will take.

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