## Digital Electronics \& Computer Engineering (E85)

Harris

Final Exam

This is a closed-book take-home exam. Electronic devices including calculators are not allowed, except on the computer question on the last page. You are permitted two $8.5 \times 11$ " sheets of paper with notes.

You are bound by the HMC Honor Code while taking this exam.
The first part of the exam is written, while the final page is done on the computer based on your E85 Lab 11. The entire Lab 11 that you use (including datapath and controller) must be your own work; it cannot, for example, include somebody else's controller. The exam is intended to be doable in 3 hours if you have prepared adequately. However, there will be no limit on the time you are allowed except that the written portion must be completed in one contiguous block of time and the computer part must be completed in another contiguous block of time. A contiguous block of time is a period of time working at a desk without breaking for meals, naps, socializing, etc. You cannot study for E85 or consult E85 resources between the two blocks of time. Please manage your time wisely and do not let the exam expand to take more time than is justified.

Return the exam to the E85 box in the Engineering Department Office no later than Wednesday 12/18 at noon.
Alongside each question, the number of points is written in brackets. All work and answers should be written directly on this examination booklet, except for printouts. Use the backs of pages if necessary. Write neatly; illegible answers will be marked wrong. Show your work for partial credit.

## Name:

$\qquad$

## Do Not Write Below This Point

Page 2:/ 4

Page 3: $\quad$ / 4
Page 4: $\quad 17$
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Page 16: / 6
Total: $\quad$ / 50
[4] Interpret $A=0 x 40 D 40000$ and $B=0 \times C 0 C 80000$ as IEEE single-precision floating point numbers. Compute their sum $\mathrm{C}=\mathrm{A}+\mathrm{B}$, and write the result as a floating-point number in hexadecimal.

## Decimal Value of A:

$\qquad$

Decimal Value of B: $\qquad$

Decimal Value of C: $\qquad$

Hexadecimal Representation of C: $\qquad$

An AND-OR-INVERT-22 (AOI22) gate computes $\mathrm{Y}=\sim(\mathrm{AB}+\mathrm{CD})$. The symbol is shown below. An AOI22 is considered one compound gate, not three individual gates.

[2] Using only an AOI22 gate and inverters, sketch a schematic for a $2: 1$ multiplexer. Let your inputs be S, D0, and D1, and your output be Y.
[2] Is it possible to perform any arbitrary function of 2 variables using a single AOI22 gate and as many inverters as you want? Explain why, or give a counterexample.

YES / NO
(explanation / counterexample)

Consider the circuit below. Notice that the circuit uses an AOI22 gate defined in the previous problem.

[4] Draw a state transition diagram for the circuit.
[3] Suppose the inputs below are applied. Sketch the behavior of the states and outputs.


B

## S1

S0
X
Y
[3] Write Behavioral Verilog code for the circuit based on your state transition diagram.

```
module final(input logic clk, reset,
    input logic a, b,
    output logic x, y);
```

endmodule

Consider the same circuit, repeated here for your convenience.

[2] How many logic elements are required to build this circuit on our Spartan FPGA?

Logic Elements $\qquad$
[3] Suppose that each input or clock pin of each gate or register has 3 fF of capacitance. (Note that the AOI22 has 4 input pins.) The X and Y outputs each drive 10 fF of capacitance. Suppose that the data signals have an average activity factor $\alpha$ of 0.1 , and reset has an activity factor of approximately 0 . The power supply voltage is $\sqrt{2} \mathrm{~V}$, and the circuit operates at 1 GHz . Compute the power consumption of the circuit.
$\qquad$
[5] Write an assembly language function to compare two strings. The answer should be 1 if the first string comes earlier in alphabetical (ASCII) order than the second, -1 if the first string comes later than the second, and 0 if the strings are identical. When the function is called, R0 and R1 contain the base address of two null-termianted strings. Return your result in R0. Hint: MVN R0, \#0 puts -1 in R0.

Use ASCII order for comparison of nonalphabetic characters. For example,

```
strcmp("Alicia", "Ben") = 1
strcmp("MIT", "HMC") = -1
strcmp("Finals", "Finals") = 0
strcmp("E85A", "E85") = -1
strcmp("cash", "ca$h") = -1 because the ASCII value for s is 115 and for $ is 36.
```

[4] Refer to the memory maps below using the I2C1 Inter-integrated circuit port. Write a C function to set the 10-bit Own Address field (OA1) of the I2C_OAR1 to 0x047 and then wait until the Receive Not Empty (RXNE) field of the I2_ISR is true. Don't rely on any libraries; define the register addresses yourself.

Table 101. I2C register map and reset values

| Offset | Register | ¢ | O-9 | $\mathbf{N}$ | $\underset{\sim}{\infty}$ | N | $\left\lvert\, \begin{gathered} \underset{N}{N} \\ \hline \end{gathered}\right.$ | $\stackrel{1}{N}$ | $\underset{\mathbf{N}}{\mathbf{N}}$ | $\stackrel{\sim}{\mathbf{N}}$ | $\mathbb{N}$ | - |  | - |  | - |  | $\stackrel{1}{7}$ | $\pm$ | $\stackrel{\sim}{\square}$ | $\stackrel{ }{\sim}$ | $F$ | 은 | 0 | $\infty$ | N | $\bullet$ | 0 | - | $\cdots$ | N | - | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0x0 | 12C_CR1 |  | ¢ |  |  |  | c |  |  | $\begin{aligned} & \underset{\sim}{U} \\ & \underset{\sim}{\mathrm{u}} \end{aligned}$ | $\begin{gathered} \underset{\sim}{\underset{\sim}{w}} \\ \underset{\sim}{\underset{\sim}{u}} \end{gathered}$ | $\begin{aligned} & z \\ & \stackrel{\rightharpoonup}{\hat{u}} \\ & \sum_{\omega}^{\infty} \end{aligned}$ |  | $\begin{aligned} & z \\ & \text { Z } \\ & \hline \end{aligned}$ | $\begin{aligned} & \underset{\sim}{u} \\ & \sum_{3}^{2} \end{aligned}$ |  |  |  | $\begin{aligned} & \underset{\sim}{U} \\ & \sum_{0}^{2} \\ & \underset{V}{x} \end{aligned}$ |  | $$ |  | NF | 3:0] |  |  |  | $\frac{\omega}{\overline{0}}$ |  |  | $\underset{\underset{\sim}{\underset{\sim}{x}}}{\underset{\sim}{\underset{2}{2}}}$ | $\stackrel{\underset{x}{\underset{~}{x}}}{ }$ | แ |
|  | Reset value |  |  |  |  |  |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0x4 | 12C_CR2 |  |  | ¢ |  |  |  |  | $\begin{aligned} & \stackrel{\text { Q}}{0} \\ & \underset{\sim}{\underset{\sim}{u}} \end{aligned}$ |  |  | NBY | TES | [7:0] |  |  |  | $\begin{aligned} & \text { 는 } \\ & \hline \end{aligned}$ | $\frac{0}{0}$ | $\begin{gathered} \frac{k}{x} \\ \frac{\alpha}{6} \\ \hline 6 \end{gathered}$ | $\begin{aligned} & \stackrel{\mathrm{r}}{\mathrm{o}} \\ & \stackrel{\rightharpoonup}{\mathrm{o}} \\ & \stackrel{\underset{\mathrm{u}}{2}}{ } \end{aligned}$ | 은 |  |  |  |  |  | ADD | [9: |  |  |  |  |
|  | Reset value |  |  |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0x8 | I2C_OAR1 |  | $\times$ | - | - | $x$ | - |  | $\Perp$ | - | - | 판 |  |  | $\ltimes$ | $\propto$ |  |  |  | - | ฯ |  | $\stackrel{\text { 山 }}{\stackrel{\rightharpoonup}{\circ}}$ |  |  |  |  | A1 | 9:0] |  |  |  |  |
|  | Reset value |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 0 |  |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0xC | I2C_OAR2 |  | $\pm$ | $\triangle$ | $\square$ | - | $\pm$ |  | $\square$ | $\square$ | 는 | 파 |  |  | $\square$ |  |  | 를 |  | r | $\simeq$ |  |  |  |  |  |  |  | [7: |  |  |  |  |
|  | Reset value |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 0 |  |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |
| 0x10 | I2C_TIMINGR | PRESC[3:0] |  |  |  | ¢ |  |  |  | $\begin{gathered} \text { SCLDEL[3:0 } \\ \text { ] } \end{gathered}$ |  |  |  | $\begin{aligned} & \text { SDADEL[3: } \\ & 0] \end{aligned}$ |  |  |  | SCLH[7:0] |  |  |  |  |  |  |  | SCLL[7:0] |  |  |  |  |  |  |  |
|  | Reset value | 0 | 0 | 0 | 0 |  |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0x14 | 12C TIMEOUTTR |  | \% | $\simeq$ |  | TIMEOUTB[11:0] |  |  |  |  |  |  |  |  |  |  |  | $\begin{aligned} & \underset{\sim}{\underset{3}{2}} \\ & \stackrel{\rightharpoonup}{3} \\ & \underset{i}{0} \end{aligned}$ |  |  |  | TIMEOUTA[11:0] |  |  |  |  |  |  |  |  |  |  |  |
|  | Reset value | 0 |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0x18 | I2C_ISR |  |  |  |  |  |  |  | ADDCODE[6:0] |  |  |  |  |  |  |  | $\underline{\underline{\square}}$ | $$ |  |  |  | $\begin{aligned} & \frac{\alpha}{\underset{\sim}{w}} \\ & \underset{\sim}{u} \\ & \underset{\sim}{u} \end{aligned}$ | $\stackrel{\alpha}{\partial}$ | $\begin{aligned} & \mathrm{O} \\ & \stackrel{\rightharpoonup}{\mathrm{x}} \end{aligned}$ | $\begin{gathered} \stackrel{r}{\Upsilon} \\ \underset{\sim}{\underset{\sim}{x}} \end{gathered}$ | $\begin{array}{\|c} \underset{U}{\mathrm{Y}} \\ \hline \mathrm{~F} \end{array}$ | $\bigcirc$ | $\begin{aligned} & \frac{4}{0} \\ & \frac{0}{6} \end{aligned}$ | $\begin{aligned} & \frac{1}{\mathbf{y}} \\ & \frac{\mathbf{y}}{\mathbf{z}} \end{aligned}$ | $\begin{aligned} & \stackrel{\alpha}{\circ} \\ & \stackrel{\alpha}{<} \end{aligned}$ |  | $\stackrel{0 \Omega}{\times}$ | $\stackrel{\text { ய }}{\text { ¢ }}$ |
|  | Reset value |  |  |  |  |  |  |  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |

Table 1. STM32F0xx peripheral register boundary addresses (continued)

| Bus | Boundary address | Size | Peripheral | Peripheral register map |
| :---: | :---: | :---: | :---: | :---: |
|  | 0x4000 7C00-0x4000 7FFF | 1 KB | Reserved |  |
|  | 0x4000 7800-0x4000 7BFF | 1 KB | CEC | Section 31.7 .7 on page 910 |
|  | 0x4000 7400-0x4000 77FF | 1 KB | DAC | Section 14.10.15 on page 291 |
|  | 0x4000 7000-0x4000 73FF | 1 KB | PWR | Section 5.4.3 on page 92 |
|  | 0x4000 6C00-0x4000 6FFF | 1 KB | CRS | Section 7.6.5 on page 147 |
|  | 0x4000 6800-0x4000 6BFF | 1 KB | Reserved |  |
|  | 0x4000 6400-0x4000 67FF | 1 KB | CAN | Section 29.9.5 on page 854 |
|  | 0x4000 6000-0x4000 63FF | 1 KB | USB/CAN SRAM | Section 30.6.3 on page 890 |
|  | 0x4000 5C00-0x4000 5FFF | 1 KB | USB | Section 30.6.3 on page 890 |
|  | 0x4000 5800-0x4000 5BFF | 1 KB | I2C2 | Section 26.7.12 on page 685 |
|  | 0x4000 5400-0x4000 57FF | 1 KB | I2C1 | Section 26.7.12 on page 685 |

void i2c_twiddling(void) \{

Consider the following program. Initially, suppose R5 contains the value $0 \times 0400$ and memory location $0 x 420$ contains the value 17 .

```
LDR R6, [R5, #0x20]
ADD R7, R6, #1
SUBS R1, R5, #42
BNE AROUND
SUB R8, R5, #30
ADD R8, R8, R7
STR R8, [R5, #0x24]
AROUND
STR R7, [R5, #0x28]
```

The program is executed on our pipelined processor with the same hazard handling you considered in class and Problem Set 10. The behavior of the pipeline for the first instruction is illustrated below. For example, in cycle 2, the value $0 \times 0400$ is read from the first port of the register file.

[1] What value is written to the register file on cycle 5?
[1] What does the ALU do on cycle 6?
[1] In which cycle is the memory written?
[1] Which memory address is written?

The ARM LDR $\operatorname{Rd}$, [ $R n$, imm]! is like an ordinary LDR but also updates the base address $\mathrm{Rn}=\mathrm{Rn}+\mathrm{imm}$. This is called a pre-indexed load. For example, if R 1 is initially $0 x 1000$, and memory location $0 \times 1008$ contains 42 , then LDR R2, [R1, \#8] puts 42 in R2 and $0 \times 1008$ in R1. In ARM machine language, the W bit of the function field is 1 for pre-indexed loads and 0 for ordinary loads. Note that $\mathrm{Ibar}=0, \mathrm{P}=1, \mathrm{U}=1, \mathrm{~B}=0$, and L $=1$ for both kinds of loads. Modify the ARM multicycle processor to support the preindexed load instruction, using as little additional hardware as feasible.
[3] Mark up the attached multicycle processor diagram and ALU to handle the new instructions.
[2] Mark up the attached multicycle controller (including state transition diagram and truth tables) to handle the new instructions.
[2] The attached multicycle memfile.s test code has highlighted modifications to test the new instruction. As compared to the memfile.s from Lab 11, it replaces the LDR instruction at $0 \times 4 \mathrm{C}$ with an a pre-indexed load.
Translate the pre-indexed command to machine language. Express your code in hexadecimal. The format for a memory instruction is given below. The cond field for ALWAYS is 1110 . Hint: $231_{10}=E 7_{16}$.


LDR R3, [R2, \#231]! $\qquad$
[1] Predict what value should be written to mem[248] at the last line of the program.

Predicted Value: $\qquad$

## Multicycle Processor



Figure 7.30 Complete multicycle processor
ALU


## Multicycle Controller



Table 7.6 Instr Decoder logic for RegSrc and ImmSrc

| Instruction | Op | Funct $_{5}$ | Funct $_{0}$ | RegSrc $_{1}$ | RegSrc $_{0}$ | ImmSrc $_{1: 0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| LDR | 01 | X | 1 | X | 0 | 01 |
| STR | 01 | X | 0 | 1 | 0 | 01 |
| DP immediate | 00 | 1 | X | X | 0 | 00 |
| DP register | 00 | 0 | X | 0 | 0 | 00 |
| B | 10 | X | X | X | 1 | 10 |


| ALUOp | Funct $_{4: 1}$ (cmd) | Functo (S) | Type | ALUControl $_{1: 0}$ | Flag $_{1: 0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | X | X | Not DP | 00 (Add) | 00 |
| 1 | 0100 | 0 | ADD | 00 (Add) | 00 |
|  |  | 1 |  |  | 11 |
|  | 0010 | 0 | SUB | 01 (Sub) | 00 |
|  |  | 1 |  |  | 11 |
|  | 0000 | 0 | AND | 10 (And) | 00 |
|  |  | 1 |  |  | 10 |
|  | 1100 | 0 | ORR | 11 (Or) | 00 |
|  |  | 1 |  |  | 10 |

; memfile.dat

| MAIN |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| SUB R0, R15, R15 | ; $\mathrm{R} 0=0$ | 1110 | 00000100 | 1111 | 0000 | 0000 | 0000 | 1111 | E04F000F | 0x00 |
| ADD R2, R0, \#5 | ; R2 = 5 | 1110 | 00101000 | 0000 | 0010 | 0000 | 0000 | 0101 | E2802005 | 0x04 |
| ADD R3, R0, \#12 | ; R3 $=12$ | 1110 | 00101000 | 0000 | 0011 | 0000 | 0000 | 1100 | E280300C | 0x08 |
| SUB R7, R3, \#9 | ; R7 = 3 | 1110 | 00100100 | 0011 | 0111 | 0000 | 0000 | 1001 | E2437009 | 0x0c |
| ORR R4, R7, R2 | ; R4 = 3 OR $5=7$ | 1110 | 00011000 | 0111 | 0100 | 0000 | 0000 | 0010 | E1874002 | $0 \times 10$ |
| AND R5, R3, R4 | ; R5 = 12 AND $7=4$ | 1110 | 0000000 | 0011 | 0101 | 0000 | 0000 | 0100 | E0035004 | 0x14 |
| ADD R5, R5, R4 | ; $\mathrm{R} 5=4+7=11$ | 1110 | 00001000 | 0101 | 0101 | 0000 | 0000 | 0100 | E0855004 | $0 \times 18$ |
| SUBS R5, R5, \#10 | ; R5 = $11-10=1$ | 1110 | 0010010 | 0101 | 0101 | 0000 | 0000 | 1010 | E255500A | 0x1c |
| SUBSGT R5, R5, \#2 | ; $\mathrm{R} 5=1-2=-1$ | 1100 | 0010010 | 0101 | 0101 | 0000 | 0000 | 0010 | C2555002 | 0x20 |
| ADD R5, R5, \#12 | R5 $=-1+12=11$ | 1110 | 0010100 | 0101 | 0101 | 0000 | 0000 | 1100 | E285500C | 0x24 |
| SUBS R8, R5, R7 | ; R8 = $11-3=8$ | 1110 | 00000101 | 0101 | 1000 | 0000 | 0000 | 0111 | E0558007 | $0 \times 28$ |
| BEQ END | ; not taken | 0000 | 10100000 | 0000 | 0000 | 0000 | 0000 | 1100 | OA00000F | 0x2c |
| SUBS R8, R3, R4 | ; $\mathrm{R} 8=12-7=5$ | 1110 | 00000101 | 0011 | 1000 | 0000 | 0000 | 0100 | E0538004 | 0x30 |
| BGE AROUND | ; should be taken | 1010 | 10100000 | 0000 | 0000 | 0000 | 0000 | 0000 | AA000000 | 0x34 |
| ADD R5, R0, \#0 | ; should be skipped | 1110 | 00101000 | 0000 | 0101 | 0000 | 0000 | 0000 | E2805000 | $0 \times 38$ |
| AROUND |  |  |  |  |  |  |  |  |  |  |
| SUBS R8, R7, R2 | ; R8 = 3-5 $=-2$ | 1110 | 0000010 | 0111 | 1000 | 0000 | 0000 | 0010 | E0578002 | 0x3c |
| ADDLT R7, R5, \#1 | ; $\mathrm{R} 7=11+1=12$ | 1011 | 00101000 | 0101 | 0111 | 0000 | 0000 | 0001 | B2857001 | 0x40 |
| SUB R7, R7, R2 | ; R7 = 12-5 = 7 | 1110 | 00000100 | 0111 | 0111 | 0000 | 0000 | 0010 | E0477002 | 0x44 |
| STR R7, [R3, \#224] | ; mem[12+224] = 7 | 1110 | 01011000 | 0011 | 0111 | 0000 | 0101 | 0100 | E58370E0 | 0x48 |
| LDR R3, [R2, \#231]! | ; |  |  |  |  |  |  |  |  |  |
| ADD R15, R15, R0 | ; PC <- PC + 8 | 1110 | 00001000 | 1111 | 1111 | 0000 | 0000 | 0000 | E08FF000 | 0x50 |
| ADD R2, R0, \#14 | ; shouldn't happen | 1110 | 00101000 | 0000 | 0010 | 0000 | 0000 | 0001 | E280200E | $0 \times 54$ |
| B END | ; always taken | 1110 | 10100000 | 0000 | 0000 | 0000 | 0000 | 0001 | EA000001 | 0x58 |
| ADD R2, R0, \#13 | ; shouldn't happen | 1110 | 00101000 | 0000 | 0010 | 0000 | 0000 | 0001 | E280200D | 0x5C |
| ADD R2, R0, \#10 | ; shouldn't happen | 1110 | 00101000 | 0000 | 0010 | 0000 | 0000 | 0001 | E280200A | $0 \times 60$ |
| END |  |  |  |  |  |  |  |  |  |  |
| STR R2, [R0, \#248] | ; mem[248] = ? | 1110 | 01011000 | 0000 | 0010 | 0000 | 1111 | 1000 | E58020F8 | 0x64 |

DO NOT PROCEED PAST THIS POINT UNTIL YOU ARE PREPARED TO CEASE ALL WORK ON THE WRITTEN PORTION AND MOVE ON TO THE COMPUTER PORTION.


## COMPUTER PORTION OF EXAM

Once you start this question, you may refer to the written portion of the exam, but may not spend any more time on the written portion or change any of your answers on that portion.

Modify your ARM multicycle processor from Lab 11 to support the pre-indexed load instruction. Modify your memfile.dat to replace the existing LDR instruction with the preindexed load.
[2] Print out your Verilog code and circle or highlight the lines you modified.
[4] Print out a simulation waveform showing at least the value being written to memory location 248 on the last cycle. Circle this value in the waveform.

